


Article

Evolution of Free Volumes in Polycrystalline BaGa₂O₄ Ceramics Doped with Eu³⁺ Ions

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Abstract: BaGa₂O₄ ceramics doped with Eu³⁺ ions (1, 3 and 4 mol.%) were obtained by solid-phase sintering. The phase composition and microstructural features of ceramics were investigated using X-ray diffraction and scanning electron microscopy in comparison with energy-dispersive methods. Here, it is shown that undoped and Eu³⁺-doped BaGa₂O₄ ceramics are characterized by a developed structure of grains, grain boundaries and pores. Additional phases are mainly localized near grain boundaries creating additional defects. The evolution of defect-related extended free volumes in BaGa₂O₄ ceramics due to the increase in the content of Eu³⁺ ions was studied using the positron annihilation lifetime spectroscopy technique. It is established that the increase in the number of Eu³⁺ ions in the basic BaGa₂O₄ matrix leads to the agglomeration of free-volume defects with their subsequent fragmentation. The presence of Eu³⁺ ions results in the expansion of nanosized pores and an increase in their number with their future fragmentation.

Keywords: ceramics; doping; free-volume defects; positron annihilation; agglomeration; fragmentation



Citation: Klym, H.; Karbovnyk, I.; Luchechko, A.; Kostiv, Y.; Pankratova, V.; Popov, A.I. Evolution of Free Volumes in Polycrystalline BaGa₂O₄ Ceramics Doped with Eu³⁺ Ions. *Crystals* **2021**, *11*, 1515. <https://doi.org/10.3390/cryst11121515>

Academic Editors: Raghvendra Singh Yadav and Anju Anju

Received: 26 October 2021

Accepted: 3 December 2021

Published: 5 December 2021

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1. Introduction

BaGa₂O₄ ceramics are considered to be promising material for use as an insulator in optoelectronic devices [1,2], as a secondary coating for plasma panels [3–5], etc. [6]. The doping of impurities in the form of rare-earth ions leads to the expansion of the functional properties of such ceramics [7]. Spinel compounds doped with transition metal ions are promising due to the number of ways to tailor the luminescence spectrum by adjusting the impurity content or by influencing the localization of the dopant in the structure.

The investigation of materials similar to BaGa₂O₄ ceramics in both undoped and doped forms is mainly focused on the study of their luminescent properties [1,8–14]. Ceramics are a double oxide belonging to the quadrilateral frame topologies that exist in multiple polymorphs, which is important for luminescence studies because it exhibits luminescence without the inclusion of rare-earth ions. However, the most interesting are rare-earth-doped BaGa₂O₄ ceramics. Most investigations of such material are limited to X-ray diffraction (XRD), optical studies, etc. [15–19]. Nevertheless, the doping of such ceramics not only leads to the modification of their luminescent properties and changes in phase composition, but also causes structural transformation [20,21]. This significantly transforms the inner structure of ceramics forming additional defect-related free volumes [22–27].

One promising method (as an alternative and addition to traditional ones) for studying the free volume in solids of different structural types is positron annihilation lifetime

(PAL) spectroscopy [28,29]. This technique has long been considered for the structural analysis of functional materials such as ceramics [30–32], glass [33,34], polymers [35,36], nanocomposites [37,38], etc. Scientific groups that are actively working in this direction have presented different approaches to the analysis of the PAL spectra of ceramic materials and their decomposition into different numbers of components [39–41]. We have also conducted a lot of research using the PAL method to study changes in free volume in spinel ceramics [42], chalcogenide glasses [43] under the influence of technological modification, etc. It was shown that functional ceramics are characterized by the decomposition of the PAL spectrum into two, three and four components depending on the developed porous structure of materials. Knowledge about the mechanisms of inner free-volume transformations is crucial for facilitating advances in the design and control of ceramics microstructure. This is required to optimize properties that enable efficient scintillation features in various applications.

It was shown that for functional ceramic materials two PAL channels are possible: the capturing of positrons by bulk defects with short and medium positron lifetimes, as well as the channel of decay of ortho-positronium (o-Ps) atoms with a long lifetime. The short-term component reflects the microstructural features of the main phase, the middle one is connected with defect-related voids near grain boundaries and the lifetime of the long-term component can estimate the transformation of nanopores. However, the study of BaGa₂O₄ ceramics using the PAL method has not yet been conducted. Therefore, the goal of this work was to study the transformations of inner free volumes (extended defects at grain boundaries and nanopores) in BaGa₂O₄ ceramics doped with different amounts of Eu³⁺ ions using the PAL method in combination with XRD and scanning electron microscopy (SEM) techniques.

2. Materials and Methods

Samples of pure BaGa₂O₄ ceramics and those with Eu³⁺ impurities were prepared using high-temperature solid-phase synthesis. Powders of BaCO₃ and Ga₂O₃ oxides with purities of 99.99% were taken as starting components for synthesis. Isopropyl CH₃-CH(OH)-CH₃ alcohol was also used in the sintering of BaGa₂O₄-based ceramics [44].

The oxide mixtures were taken at a stoichiometric ratio of 1:1 mol per 2 g of raw material. The content of the Eu³⁺ ions (Eu₂O₃ with a purity of 99.99%) was determined to replace the equivalent molar content of Ga and Ba. The amount of Eu³⁺ ions was 0, 1, 3 and 4 mol.%. The oxide mixture was stirred thoroughly in an agate solution for 6 h with the addition of isopropyl alcohol. The obtained raw material was air-dried for 1 h at a temperature of 80 °C. After that, the raw material was pressed under a pressure of 150 kg/cm², obtaining workpieces with a diameter of 6 mm and a thickness of 1.5 mm. The blanks were placed on a platinum substrate and annealed in a furnace at 1200 °C for 12 h in air. In the next stage, annealing was performed at 1300 °C for 5 h. The final ceramic samples were in the form of tablets with a diameter of 4 mm and a thickness of 1 mm.

X-ray examinations were performed using a STOE STADI P (STOE & Cie GmbH, Darmstadt, Germany) diffractometer. The source of the X-rays was a copper anode tube with Cu K α 1 radiation ($\lambda = 1.5406 \text{ \AA}$). The investigated range of diffraction angles used was from 2 to 100° with a minimum measurement step of 0.005°. The microstructural study of grains, grain boundaries and pores in the BaGa₂O₄ ceramics doped with Eu³⁺ ions was investigated using a high-resolution ZEISS Ultra Plus SEM (Carl Zeiss Microscopy Deutschland GmbH, Zeiss, Germany) with two secondary electron detection systems including elementary compositions analysis.

The ORTEC system with a ²²Na isotope as a positron source was used for PAL measurements. Investigations were performed at 22 °C and a relative humidity of 35% for two identical ceramic samples placed in a sandwich configuration as described in [45].

The measured PAL spectra were calculated using LT software [46] in a three-component fitting procedure (lifetimes τ_1 , τ_2 , τ_3 and intensities I_1 , I_2 , I_3) for spinel ceramics with a branched porous structure [45]. Parameters, such as the average lifetime of positrons τ_{av} ,

the lifetime of positrons in defect-free bulk τ_b and the rate of positron trapping in defects κ_d , were obtained using a two-stage positron trapping model [45]. We also determined the $\tau_2 - \tau_b$ difference (which describes the size of the free-volume defects where positrons are trapped) and the τ_2/τ_b ratio (which correlates with the nature of defects). Using the lifetime of the third component, the radii of the nanopores (R_3) were determined using the Tao–Eldrup model [47].

3. Results and Discussion

According to the results of the XRD investigations [44], the initial undoped BaGa_2O_4 ceramics contain three phases: 34.2 wt.% of the main BaGa_2O_4 phase, 58.5 wt.% of the additional $\text{Ba}_{2.84}\text{Ga}_{11.32}\text{O}_{19.82}$ phase and 7.3 wt.% of the Ga_2O_3 phases. The BaGa_2O_4 ceramics with 1 mol.% Eu^{3+} ions are single-phase. The BaGa_2O_4 ceramics with a 3 and 4 mol.% impurity of Eu^{3+} ions contain two phases: 97.3 and 96.7 wt.% of the BaGa_2O_4 phase as well as 2.7 and 3.3 wt.% of the additional Eu_3GaO_6 phase, respectively. The results of the detailed XRD analysis using Rietveld’s method are represented in Table 1.

Table 1. Phase composition and Rietveld refined parameters for undoped and Eu^{3+} -doped BaGa_2O_4 ceramics.

Sample	Number of Phases	Phases, Lattice Parameters, Weight Fraction
BaGa_2O_4	3 phases: BaGa_2O_4 , $\text{Ba}_{2.84}\text{Ga}_{11.32}\text{O}_{19.82}$ and Ga_2O_3	BaGa_2O_4 : $a = 18.619(1) \text{ \AA}$, $c = 8.670(1) \text{ \AA}$ fraction 34.2 wt.% $\text{Ba}_{2.84}\text{Ga}_{11.32}\text{O}_{19.82}$: $a = 15.807(1) \text{ \AA}$, $b = 11.687(1) \text{ \AA}$, $c = 5.136(1) \text{ \AA}$, $\beta = 107.62(1) \text{ \AA}$, fraction 58.5 wt.% Ga_2O_3 : $a = 12.213(4) \text{ \AA}$, $b = 3.042(1) \text{ \AA}$, $c = 5.810(2) \text{ \AA}$, $\beta = 103.65(3) \text{ \AA}$, fraction 7.3 wt.%
$\text{BaGa}_2\text{O}_4 + 1 \text{ mol.\% Eu}^{3+}$	1 phase: $(\text{Ba,Eu})\text{Ga}_2\text{O}_4$	$(\text{Ba,Eu})\text{Ga}_2\text{O}_4$: $a = 18.605(1) \text{ \AA}$, $c = 8.670(1) \text{ \AA}$, fraction 100 wt.%
$\text{BaGa}_2\text{O}_4 + 3 \text{ mol.\% Eu}^{3+}$	2 phases: BaGa_2O_4 , Eu_3GaO_6	BaGa_2O_4 : $a = 18.620(1) \text{ \AA}$, $c = 8.658(1) \text{ \AA}$, fraction 97.3 wt.% Eu_3GaO_6 : $a = 9.026(2) \text{ \AA}$, $b = 11.344(2) \text{ \AA}$, $c = 5.496(1) \text{ \AA}$, fraction 2.7 wt.%
$\text{BaGa}_2\text{O}_4 + 4 \text{ mol.\% Eu}^{3+}$	2 phases: BaGa_2O_4 , Eu_3GaO_6	BaGa_2O_4 : $a = 18.622(1) \text{ \AA}$, $c = 8.658(1) \text{ \AA}$, fraction 96.7 wt.% Eu_3GaO_6 : $a = 9.031(2) \text{ \AA}$, $b = 11.343(2) \text{ \AA}$, $c = 5.497(1) \text{ \AA}$, fraction 3.3 wt.%

Generalized XRD patterns for undoped BaGa_2O_4 ceramics and those doped with Eu^{3+} ions, in comparison with the diffraction pattern of BaGa_2O_4 in the ICSD reference data file, are shown in Figure 1. The availability of the main phase in the studied ceramics indicates peaks at the reflection angle 2θ of 28.12° .

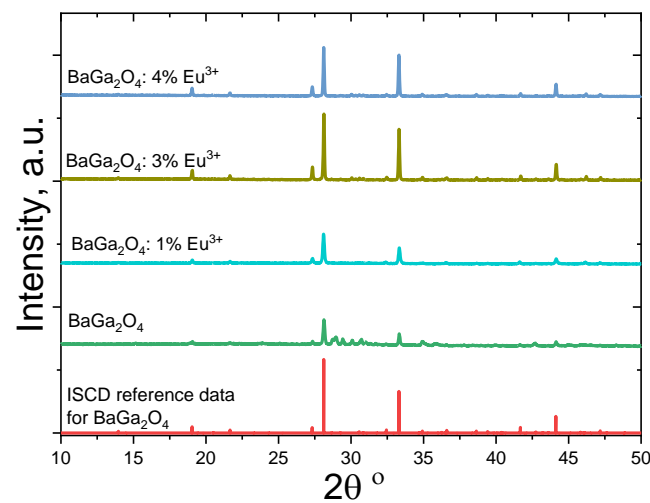


Figure 1. XRD patterns for undoped and Eu^{3+} -doped BaGa_2O_4 ceramics in comparison with ICSD reference data for BaGa_2O_4 .

As can be seen from the SEM images, both undoped BaGa_2O_4 ceramics (Figure 2a) as well as ceramics with 1 mol.% Eu^{3+} ions (Figure 2b) have a fairly branched structure of grains, grain boundaries and pores of different forms and shapes [45]. Samples of these ceramics are characterized by a small grain size and homogeneity in the morphology of the structure. The presence of Eu^{3+} ions leads to an increase in the pore size of the initial BaGa_2O_4 ceramics, the formation of grain agglomerates and their further growth. In addition, in both cases there is the formation of micro- and nanosized crystals on the grain surface.

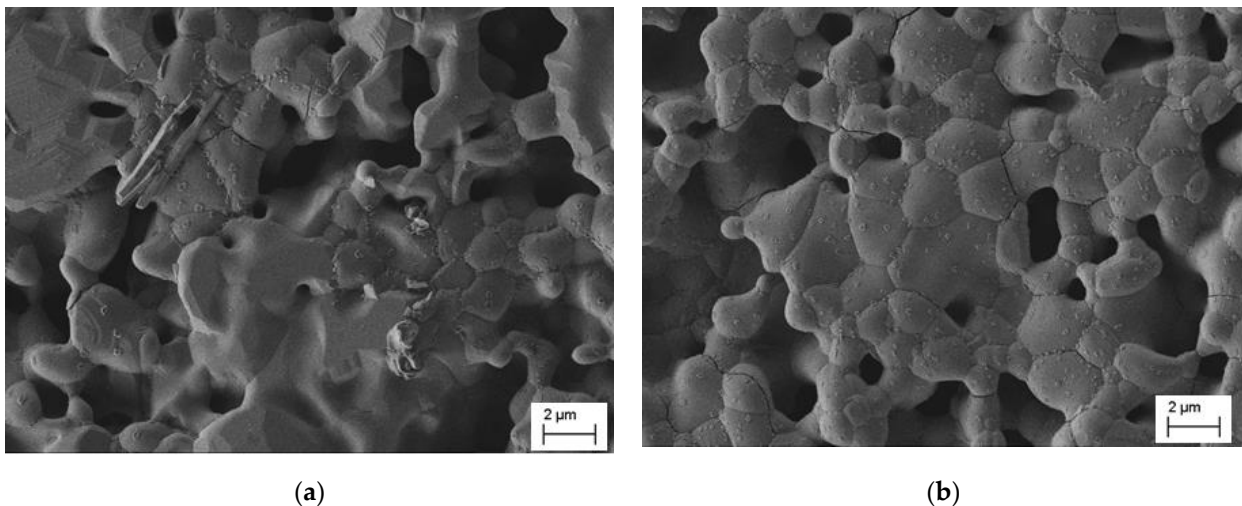


Figure 2. SEM images for undoped (a) and Eu^{3+} -doped (b) BaGa_2O_4 ceramics.

In addition, the elemental composition of the studied ceramic samples was evaluated using the method of energy-dispersion X-ray (EDX) spectroscopy for selected areas (Figure 3).

It is known that the accuracy of the EDX technique depends on the nature of the sample and other factors so only clearly defined peaks were analyzed. As can be seen from Figure 3a, elements in the BaGa_2O_4 compound are evenly distributed over the volume of crystallites, and there are reflexes of the main elements of the material. However, in the sample of BaGa_2O_4 ceramics doped with 1 mol.% Eu^{3+} ions (Figure 3b), their percentage was not established (despite the presence of Eu-reflexes). Obviously, such a small number of Eu^{3+} ions is not enough to identify the selected area. For BaGa_2O_4 ceramics with 3 mol.% Eu^{3+} ions, the presence of the latter increases to 0.74% (Figure 3c), while a further rise in the

content of impurities (to 4 mol.% Eu^{3+} ions) leads to a significant increase in the material to 4.88% (Figure 3d, Table 2). Thus, the obtained results indicate the successful incorporation of Eu^{3+} ions into the BaGa_2O_4 matrix, especially if their concentration exceeds 1 mol.%.

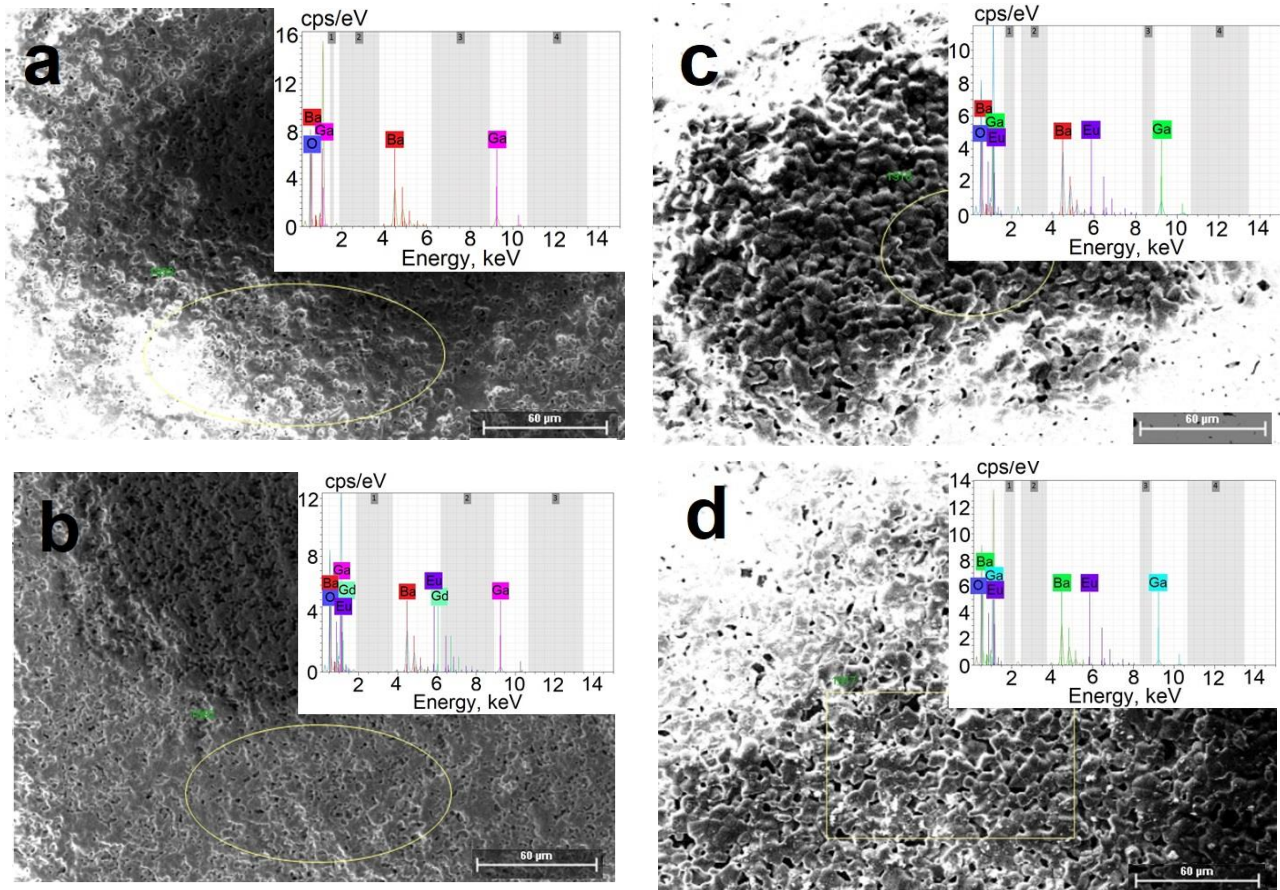


Figure 3. Microstructure of the selected areas and elemental composition of the undoped BaGa_2O_4 ceramics (a) and those doped with 1 mol.% (b), 3 mol.% (c) and 4 mol.% of Eu^{3+} ions (d).

Table 2. Elemental composition of the undoped and Eu^{3+} -doped BaGa_2O_4 ceramics.

Sample	Mass, %				Atom, %			
	O	Ga	Ba	Eu	O	Ga	Ba	Eu
BaGa_2O_4	16	34	30	-	59	28	13	-
$\text{BaGa}_2\text{O}_4 + 1 \text{ mol.}\% \text{Eu}^{3+}$	17	16	29	-	71	15	14	-
$\text{BaGa}_2\text{O}_4 + 3 \text{ mol.}\% \text{Eu}^{3+}$	16	30	44	0.74	59	25	15	0.28
$\text{BaGa}_2\text{O}_4 + 4 \text{ mol.}\% \text{Eu}^{3+}$	16	25	32	4.88	61	22	15	1.98

Obviously, the presence of different amounts of Eu^{3+} ions in the ceramic BaGa_2O_4 matrix will modify their inner free volume. Extended defects formed in ceramic materials and mainly localized near grain boundaries are also due to the release of additional phases. The PAL method was used to study such defect-related free volumes in undoped and Eu^{3+} -doped BaGa_2O_4 ceramics.

The fitting parameters of PAL spectra for the studied ceramics calculated within a three-component procedure are presented in Table 3. It is established that with rising Eu^{3+} content in the BaGa_2O_4 matrix, an increase in the lifetime τ_1 and intensity I_1 of the first short-term component is observed. Most probably, the structure of the mail phase of the ceramics is improved. However, when the Eu^{3+} ions increase to 4 mol.%, the opposite trend occurs. The lifetime τ_2 of the second component increases and intensity I_2 decreases

with Eu^{3+} content (to 3 mol.%), while a further rise in Eu^{3+} ions (to 4 mol.%) leads to a decreased τ_2 and an increased I_2 .

Table 3. Lifetimes and intensities for undoped and Eu^{3+} -doped BaGa_2O_4 ceramics obtained in three-component fitting procedure.

Sample	$\tau_1 (\pm 0.002)$, ns	$I_1 (\pm 0.1)$, %	$\tau_2 (\pm 0.001)$, ns	$I_2 (\pm 0.1)$, %	$\tau_3 (\pm 0.001)$, ns	$I_3 (\pm 0.1)$, %
BaGa_2O_4	0.200	83.3	0.424	14.9	2.196	1.8
$\text{BaGa}_2\text{O}_4 + 1 \text{ mol.}\% \text{Eu}^{3+}$	0.206	85.0	0.450	13.2	2.289	1.8
$\text{BaGa}_2\text{O}_4 + 3 \text{ mol.}\% \text{Eu}^{3+}$	0.212	89.9	0.550	7.9	2.390	2.2
$\text{BaGa}_2\text{O}_4 + 4 \text{ mol.}\% \text{Eu}^{3+}$	0.201	83.3	0.411	14.4	2.157	2.4

As noted in [42,45], the lifetime τ_2 of the second component should be associated with the capture of positrons by defect-related free volumes. According to XRD data, undoped BaGa_2O_4 ceramics contain a large number of additional phases. As shown by the SEM method, these phases are unevenly distributed in the volume of the ceramic and are mainly localized near the grain boundaries. The extracted phases play the role of special centers of positron capture in the volume of ceramics. Since undoped BaGa_2O_4 ceramics contain two additional phases, positrons in such samples will be better captured.

The lifetime τ_2 correlates with the size of the free-volume defects, where positrons are captured, and the intensity correlates with their number. Thus, when the Eu^{3+} content increases to 3 mol.%, the agglomeration of free-volume defects occurs, while the supersaturation of the BaGa_2O_4 matrix with Eu^{3+} (up to 4 mol.%) leads to their fragmentation. The identified trends (Table 4) correlate with the positron trapping parameters calculated within the two-state positron trapping model [45]. Schematically, the evolution of defect-related free volumes near grain boundaries with increasing Eu^{3+} ions in BaGa_2O_4 ceramics is shown in Figure 4.

Table 4. Positron trapping parameters and nanopore radius for undoped and Eu^{3+} -doped BaGa_2O_4 ceramics.

Sample	τ_{av} , ns	τ_b , ns	κ_d , ns^{-1}	$\tau_2 - \tau_b$, ns	τ_2/τ_b	R_3 , nm
BaGa_2O_4	0.234	0.218	0.40	0.21	1.95	0.306
$\text{BaGa}_2\text{O}_4 + 1 \text{ mol.}\% \text{Eu}^{3+}$	0.239	0.222	0.35	0.23	2.02	0.314
$\text{BaGa}_2\text{O}_4 + 3 \text{ mol.}\% \text{Eu}^{3+}$	0.240	0.223	0.23	0.33	2.46	0.322
$\text{BaGa}_2\text{O}_4 + 4 \text{ mol.}\% \text{Eu}^{3+}$	0.232	0.218	0.37	0.19	1.89	0.302

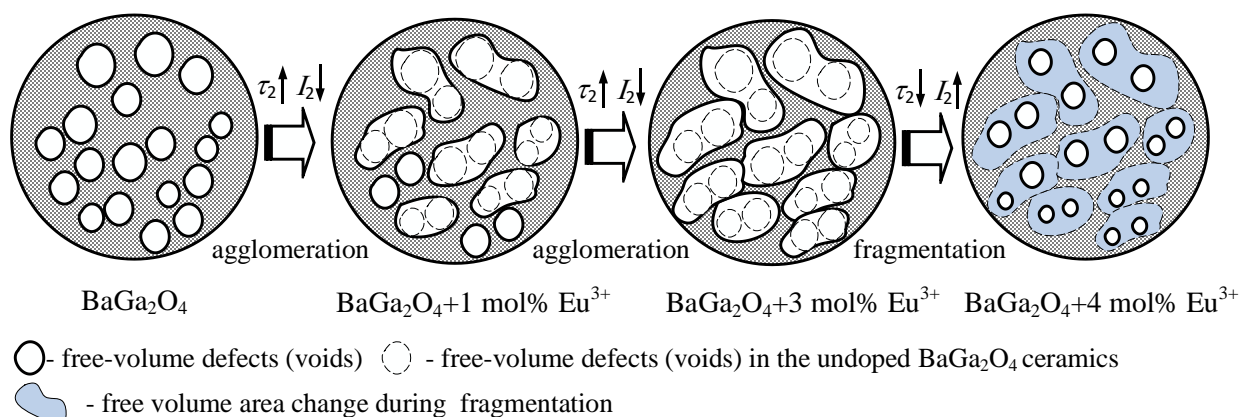


Figure 4. Diagram explaining the evolution of defect-related voids in BaGa_2O_4 ceramics caused by Eu^{3+} doping.

As mentioned above, the lifetime of the second component correlates with the size of the free-volume defect, while its intensity is defined by the amount of these defects. The agglomeration process is reflected in the increase in the second component's lifetime and in the decrease in its intensity. Solid lines in Figure 4 show existing voids in the sample,

and dotted lines indicate voids in the initial ceramics. This schematically illustrates the process when two smaller voids are joined to form a larger one.

As can be seen from Table 3, lifetime τ_2 increases from 0.424 ns in BaGa_2O_4 ceramics to 0.450 ns in BaGa_2O_4 ceramics containing 1 mol.% Eu^{3+} ions, and intensity decreases from 14.9 to 13.2%. In Figure 4, it is schematically demonstrated that most voids were agglomerated, though there were some left unchanged. Generally, the number of voids is smaller and the overall volume of the voids is larger. For BaGa_2O_4 ceramics doped with 3 mol.% Eu^{3+} ions, agglomeration is also the case, and the lifetime of the second component keeps increasing up until 0.550 ns, whereas intensity goes down to 7.9%. It is schematically shown that the voids in BaGa_2O_4 ceramics with 1 mol.% Eu^{3+} ions were unchanged; in BaGa_2O_4 ceramics with 3 mol.% Eu^{3+} ions, they were involved in agglomeration. That is why the number of voids decreased even more and the overall void volume became larger. For BaGa_2O_4 ceramics with 4 mol.% Eu^{3+} we observe the opposite—fragmentation of free-volume defects occurs. These changes are manifested in the decrease in τ_2 lifetime and the increase in I_2 intensity. In Figure 4, the region where free-volume voids change compared to BaGa_2O_4 ceramics with 3 mol.% Eu^{3+} ions due to fragmentation is shown in blue. The intensity I_2 for BaGa_2O_4 ceramics with 4 mol.% Eu^{3+} ions is close to the I_2 for undoped BaGa_2O_4 ceramics, but the lifetime τ_2 is shorter. This is evidence of the smaller overall size of free-volume defects in BaGa_2O_4 ceramics with 4 mol.% Eu^{3+} ions.

The third long-term component of the PAL spectrum (the second channel of positron annihilation with lifetime τ_3 and intensity I_3) is associated with the o-Ps decaying in nanopores [45]. As can be seen from Table 3, lifetime τ_3 and intensity I_3 increase with Eu^{3+} content in the BaGa_2O_4 ceramics (to 3 mol.%). However, when the amount of Eu^{3+} ions rises to 4 mol.%, the lifetime τ_3 decreases and the intensity I_3 continues to increase. It is obvious that the presence of Eu^{3+} ions in the ceramic matrix leads to the expansion of nanosized pores and an increase in their number. However, the supersaturation of ceramics with doped ions (to 4 mol.%) results in the fragmentation of nanopores. The obtained trends are reflected in the radius of nanopores R_3 (Table 4) calculated using the Tao–Eldrup model. This process is schematically shown in Figure 5.

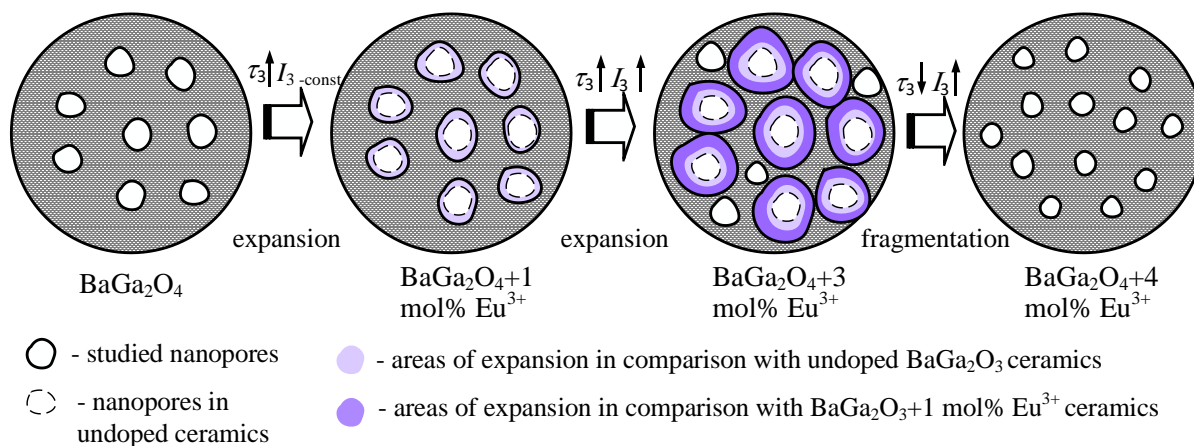


Figure 5. Diagram explaining the evolution of nanopores in BaGa_2O_4 ceramics caused by Eu^{3+} doping.

Adding 1 mol.% Eu^{3+} to the BaGa_2O_4 ceramics is reflected in the increased lifetime of the third component (up to 2.289 ns) at a constant intensity I_3 as compared to the undoped ceramics. This confirms the process of nanopore volume expansion. Further increase in Eu^{3+} content up to 3 mol.% facilitates an increase in both lifetime τ_3 and intensity I_3 , pointing at the continuation of the nanopore expansion process with simultaneous new pore creation. However, for BaGa_2O_4 ceramics with 4 mol.% Eu^{3+} ions, the opposite fragmentation process takes place, which can be described as a decreased lifetime of the third component and its increased intensity. Total nanopore volume is smaller than it is for undoped ceramics (see Table 3), thus indicating the excess character of such Eu^{3+} doping.

Thus, PAL spectroscopy can be a tool that allows us to assess the ability of Eu penetration into ceramic grains. The sites of Eu^{3+} ions define the positron trapping rate, and related structural transformations can be analyzed using positron component parameters, which change depending on the concentration of doping ions. This method can also be used to determine the size of nanopores in undoped and doped ceramic materials.

4. Conclusions

The structural features and evolution of free-volume defects in BaGa_2O_4 ceramics obtained by solid-phase synthesis from the initial BaCO_3 and Ga_2O_3 components with the addition of different amounts of Eu_2O_3 content (1, 3 and 4 mol.%) were investigated. The structural features of ceramics were studied using XRD as well as SEM with an EDX elemental analysis. It is established that, according to the quantitative analysis of the elemental composition, samples of the undoped BaGa_2O_4 ceramics have the largest deviations from the stoichiometric composition; they have three phases. Such processes are apparently caused by the evaporation of the constituent synthesis powders during the annealing process at high temperatures. The detected signs correlate with the XRD data.

Additional phases in ceramics are mainly localized near the grain boundaries and create defective centers for positron capture studied by PAL spectroscopy. Analyzing the second component of the PAL spectra for the undoped and Eu^{3+} -doped BaGa_2O_4 ceramics, it was shown that an increase in Eu^{3+} content from 1 to 3 mol.% leads to the agglomeration of free-volume defects near the grain boundaries of ceramics. At the same time, nanopores in ceramics expand and their number increases. Further increase in the content of Eu^{3+} ions is accompanied with the fragmentation of both free-volume defects and nanopores.

Results obtained by PAL spectroscopy can serve as a research base for the development of independent complementary methods for studying nanosized free volumes in ceramic materials, including neutron and heavy ion irradiated MgAl_2O_4 spinels [22,27,48], Si_3N_4 [49], Ge_3N_4 [50] and AlN [51–53], which are especially promising as diagnostic materials for nuclear applications. Other interesting and very important areas are the understanding of porosity, its development and transformation in electrochemical and other devices for energy conversion [54–64].

Author Contributions: Writing—original draft preparation, H.K.; writing—review and editing, I.K., V.P. and A.I.P.; investigation of ceramics, H.K., Y.K., A.L. and I.K.; treatment of experimental results, H.K. and Y.K.; project administration, A.I.P. All authors have read and agreed to the published version of the manuscript.

Funding: This work was supported by the Ministry of Education and Science of Ukraine (project for young researchers No. 0119U100435) for H.K. and Y.K.; the National Research Foundation of Ukraine (project 2020.02/0217) for I.K. and H.K. as well as by the Latvian research council via the Latvian National Research Program under the topic “High-Energy Physics and Accelerator Technologies”, Agreement No: VPP-IZM-CERN-2020/1-0002, for V.P. and A.I.P.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: The data presented in this study are available on request from the corresponding author.

Acknowledgments: H.K. and Y.K. would like to thank A. Ingram for assistance in PAL experiments. The authors thank E.A. Kotomin and M. Brik for the many useful discussions. The research was (partly) performed in the Institute of Solid State Physics, University of Latvia ISSP UL. ISSP UL as the Center of Excellence is supported through the Framework Program for European universities Union Horizon 2020, H2020-WIDESPREAD-01–2016–2017-TeamingPhase2 under Grant Agreement No. 739508, CAMART2 project.

Conflicts of Interest: The authors declare no conflict of interest.

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